

2.1 - Units of Area and Volume

February 14, 2017 10:34 AM

Area

The paintable space

Units: Square Units, units²

Example: m², km², cm², ft², in²



Volume

The fillable space

Units: Cubic Units, units³

Example: m³, km³, cm³, ft³, in³



Area and Volume Formulas

Area of a Rectangle

Volume of a Cube

Area and Volume Formulas

Area of a Rectangle

$$\text{Area} = L \times W$$

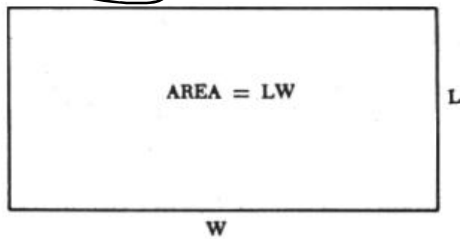
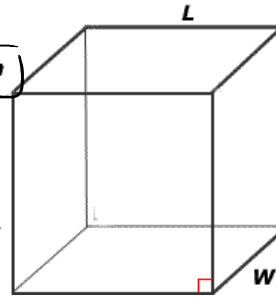


FIGURE 1-5. A rectangle.

Volume of a Cube

$$\text{Volume} = L \times W \times h$$

Like a rectangular solid, multiply the length, times the width times the height.



The only difference between these units and those we have been using before is the little ² or ³. These are exponents and signify how many of each unit is present.

m^3 : READ "meters cubed" or "Cubic meters"

$$m^3 = (m)(m)(m)$$

in^2 : READ "inches squared" or "square inches"

$$in^2 = (in)(in)$$

Let's do some conversions with these units.

Examples:

Calculate the Area in square feet and square yards of a rectangle that is 15in by 23in.



$$\text{Area} = 15in \times 23in$$

$$= 345 in^2$$

$$= 345 \cancel{(in)} \cancel{(in)} \times \frac{1ft}{12in} \times \frac{1ft}{12in}$$

$$= 345 \frac{ft^2}{(12)(12)}$$

$$= \underline{\underline{2.4 ft^2}}$$

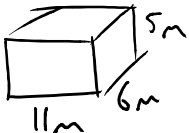
$$1ft = 12in$$

$$2.4 \cancel{ft^2} \times \frac{1yd}{3ft} \times \frac{1yd}{3ft}$$

$$= \underline{\underline{0.266 yd^2}}$$

★ When converting Areas do your conversions twice

Calculate the Volume of a rectangular prism that is 5m by 6m by 11m. Find the volume in cubic feet.



$$V = L \times W \times h$$

$$= 11 \times 6 \times 5$$

$$V = \underline{\underline{330 m^3}}$$

$$1m = 3.28ft$$

$$= 330 \cancel{(m)} \cancel{(m)} \cancel{(m)} \times \frac{3.28ft}{1m} \times \frac{3.28ft}{1m} \times \frac{3.28ft}{1m}$$

$$= 330 \times (3.28)^3 ft^3$$

$$= 11645 ft^3$$

$$= \underline{\underline{11645 \text{ ft}^3}}$$

A cube (all side lengths equal) has a volume of 7.628 in^3 . Calculate the length of one side in centimetres.

Save for
Thursday

A unknown shape has an area of 607 km^2 . What is the area in square miles?

$$1 \text{ mi} = 1.609 \text{ km}$$

$$607 \text{ km}^2$$

$$607 \cancel{\text{km}} \times \cancel{\text{km}} \times \frac{1 \text{ mi}}{1.609 \cancel{\text{km}}} \times \frac{1 \text{ mi}}{1.609 \cancel{\text{km}}} = \underline{\underline{234 \text{ mi}^2}}$$

Other units for Area and Volume

Acres

$$1 \text{ Acre} = 43560 \text{ ft}^2$$

Litres

$$1 \text{ Litre} = 1000 \text{ cm}^3$$

Example: How many square feet are in 10 acres of land?

$$10 \cancel{\text{acres}} \times \frac{43560 \text{ ft}^2}{1 \cancel{\text{acres}}} = \underline{\underline{435600 \text{ ft}^2}}$$

Only use our
conversion
formula once

Example: How many cubic centimeters is a can of pop (350mL).

$$\text{remember } 1 \text{ m} = 0.001$$

$$1 \text{ L} = 1000 \text{ cm}^3$$

$$350 \text{ mL} = (350)(0.001) \text{ L}$$

$$= 0.350 \text{ L}$$

$$0.350 \cancel{\text{L}} \times \frac{1000 \text{ cm}^3}{1 \cancel{\text{L}}} = \underline{\underline{350 \text{ cm}^3}}$$

Only use our
conversion formula
once

$$0.350\cancel{\text{L}} \times \frac{1000\text{cm}^3}{1\cancel{\text{L}}} = \underline{\underline{350\text{cm}^3}}$$

conv.
Once

Homework
Ch2.1, Page 61, Q:1-11odd, 12

Bathroom / water